Site Diversity Gain for Earth-to-Satellite Links Using Rain Intensity Measurement

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Abstract
Site diversity technique is effective method to overcome rain attenuation, mostly in the tropics where high precipitation is predominant. The method is analyzed based on measurements in two locations separated by 37.36 Km in Malaysia. From concurrent measured rain intensities of two locations at IIUM and UKM for one year, it was found that only ten concurrent events had occurred containing highest rain intensities of 18 mm/h with outage probability of 0.00154% on two locations out of about 381 events experienced over one year period. These findings will be very useful for Earth-to-satellite link designers to improve reliability by applying site diversity as a rain fade mitigation technique at any frequency.

Keywords: Site diversity technique, Rain intensity, Site diversity gain, Prediction models

1. Introduction
Microwave links that use frequency higher than 10 GHz have a serious problem with weather, primarily rain. The rain causes attenuation to communication signal through the rain fall, which is directly proportional to the frequency [1]. It may be too severe for a long time causing service disruptions. This problem can be overcome directly by providing appropriate power margins for the system in two directions uplink and downlink. This technique can achieve its results by either increasing the antenna size or raising the radio transmission power. The two methods may be used together to encounter the problem. Limitations on the communication satellite transmission power and base station radiated power, imposed by international agreements, and are assumed to be the main obstacle to increasing the radio transmission power. Most likely, these limitations will affect high frequencies in the Ku, Ka and V bands, if the attenuation exceeds the available power margin. Hence, the need to develop alternative techniques to deal with the acute attenuation conditions and improves the performance of the link. Different methods are available to overcome propagation effects. Frequency bands, system objective and network geometry are the parameters that should be taken into account to choose a suitable technique to mitigate the propagation effects. [2-6].

Diversity is one of the best techniques used in satellite communications to counteract the effects of link fading [7, 8]. The diversity can be defined as the repetition or redundancy of information. When using diversity techniques, the receiver makes the diversity decisions while the transmitter is unaware of them [9]. The efficiency of diversity techniques stem from the fact that fade of the branches is considered independent or their envelopes are uncorrelated. There are five widely used techniques of diversity in practice today, namely; site, frequency, time, orbital and polarization [9, 10].

Site diversity is the use of two or more connected receivers to reduce or evade rain effects on downlink throughout periods of heavy rainfall on one path of the earth to satellite paths. Site diversity enhances the satellite communications reliability. Furthermore, site diversity improves overall satellite link performance by exploiting the limited extent and size of the intense cell [11]. This technique exploits the physical fact that the rain structure is not uniform spatially and that most likely the intense rain cells cover a limited area. The comparison between received signals of two or more sites and selecting the signal has least attenuation is achieved by the operating center [12]). In addition, the switched signal has less attenuation among the received signals where the probability of heavy rainfall occurs at the same time on all sites is very low, this probability decreases with the distance between sites increases [10],[13].

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The models used to predict the site diversity performance are divided into empirical prediction and physical-mathematical models [14]. The high cost and complex interconnectivity are assumed the downside to this technique.

There are a number of variable factors involved while applying this technique, namely: site separation, frequency, elevation angle, baseline orientation angle, polarization angle, and wind direction. The impact of site diversity technique on the performance of system can be determined by finding the statistical rain attenuation for a reference signal and diversity joints. The diversity gain, $G_{SD}(P)$, is the difference between the attenuation values at % time [15].

$$G_{SD}(P) = A_s(P) - A_j(P)$$

where $A_s$ and $A_j$ are the single site and joint attenuation values at the probability in percentage respectively. Figure 1 depicts the diversity gain prediction.

![Figure 1. Definition of diversity gain](image)

Two tipping bucket rain gauges with 0.2 mm and 0.1 mm resolutions were also installed in IIUM and UKM respectively. For these two locations separated by 37.36 km, the rain rate were measured synchronously for one year period to analyse site diversity mitigation.

2. Prediction Models

This section will discuss previous models done on site diversity techniques. Some climates studied in these works differ from Malaysian climate but within the frequency band of interest that is Ku-band and above. In addition, there are other research works that were carried out at different frequency bands, and were done in tropical climate.

2.1. Hodge Model

The study proposes an empirical model to estimate diversity gain for satellite links. The proposed model is a function of the distance separating earth terminals, signal frequency, elevation angle, and angle between the baseline and the path azimuth. The authors of this study base their analysis on the results of 34 diversity experiments, which have been conducted in Canada, England, Japan, and the United States over a period of 10 years. The model is expressed by the following equation [16].

$$G(D, f, \theta, \beta) = G_D G_f G_\theta G_\beta$$

where
\( G_D = a(1 - e^{-bD}) \)
\( a = 0.64A - 1.6(1 - e^{-0.114}) \)
\( b = 0.585(1 - e^{-0.0984}) \)
\( G_f = 1.64e^{-0.025f} \)
\( G_\theta = 0.00492 \theta + 0.834 \)
\( G_\beta = -0.0017 \beta + 0.887 \)

where \( A \) is the rain attenuation (dB) of a single site, \( D \) is the site separation (km), \( f \) is the operating frequency (GHz), \( \theta \) is the elevation angle (degrees) of the link path and \( \beta \) is the orientation of baseline in relation to the transmission path.

2.2. ITU-R Model

The diversity gain (dB) according to ITU-R [17] is represented as a product of the gains contributed by spatial separation \( G_d \), frequency \( G_f \), elevation angle \( G_\theta \) and baseline dependent term \( G_\beta \).

\[
G_{sd} = G_d G_f G_\theta G_\beta
\]

where
\[
G_D = a(1 - e^{-bD})
\]
\( a = 0.78A - 1.9(1 - e^{-0.114}) \)
\( b = 0.59(1 - e^{-0.14}) \)
\( G_f = 1.64e^{-0.025f} \)
\( G_\theta = 1 + 0.006\theta \)
\( G_\beta = 1 + 0.002\beta \)

The distance separating the two sites, \( d \) is in kilometers; \( A \) is the path rain attenuation in decibels, \( f \) is the frequency in gigahertz, \( \theta \) is the elevation angle of the link path in degrees, and \( \beta \) is the angle made by the azimuth of the propagation path with respect to the baseline between the sites, chosen such that \( \beta \leq 90^\circ \).

2.3. Panagopoulos Model

According to [18] simple formulas are proposed to estimate the gain as a result of the use of site diversity method. The diversity gain model underwent wide testing. It is validated for site diversity system separated by distance is below 15 km. The model can be expressed by the following equation

\[
G_{sd} = A_s G_D G_f G_\theta G_\beta
\]

where \( A_s \) (decibels) presents the attenuation of the single site. Each factor is calculated according to
\[
A_s = 8.19A_s^{0.0004} + 0.1809A_s - 8.2612
\]
\( G_D = \ln(3.610 D) \)
\( G_f = \exp(-0.0006f) \)
\( G_\theta = 1.234(1 - \theta^{-0.356}) \)
\( G_\beta = 1 - 0.00006\beta \)
2.4 Nagaraja and Otung Model

The study [19] develops an empirical model for the statistical prediction of dual site
diversity gain, using rain data collected from the Nimrod weather system over 46 months. The
study's main contribution lies in incorporating exceedance time percentage and extremely high
frequency bands in the range of 16 GHz to 50 GHz. The model is a function of several
parameters, including time percentage of average year, the distance between sites (km), the
orientation of the baseline (degrees), the frequency (GHz) and the elevation angle (degrees).
The prediction model is expressed in the following equation

\[ G_{SD} = G_{f}G_{\theta} \]  

where \( G_{f} \) refers to the site diversity gain as a function of the link frequency, while the \( G_{\theta} \) refers
to the site diversity gain as function of elevation angle and \( G_{p,d,\beta} \) is a function of the time
percentage of average year, site separation and baseline orientation. The final model can be
expressed by

\[ G_{p,d,\beta,f,\theta} = (2.92 \times 10^{-2} + 5.67 \times 10^{-4} D) f^{1.19} \exp\left(\theta / \rho \right) - 0.546 \ln(\rho) 
+ d \ln(\rho) - 2.55 \sin\theta + 1.45 \sin^2 \theta \]  

where \( b \) and \( d \) are parameters that depend on values of site separation and baseline orientation
[19].

2.5. Semire Model

In [20][23], authors developed a prediction model using rain attenuation measurements
and TRMM radar data collected in five Southeast Asian countries. The study introduces two
improvements on an existing model, namely; the inclusion of low elevation angles and a high
link frequency up to 70 GHz. The new model's performance was validated using three existing
site diversity models while varying link parameters. Based on this validation, the authors show
that the proposed model can be used to predict site diversity gains in relation to site separation
and elevations angle with better accuracy, as compared to the three examined models. The
proposed model is a function of, \( d \): the separation distance in km, \( A_{s} \): the single-site attenuation
in dB, \( f \): the link frequency in GHz, \( \theta \): the angle of elevation in degrees and \( \beta \): the baseline
orientation angle in degrees.

The process followed by the proposed prediction model is similar to that of the Hodge model;
however it employs expressions and coefficients that are more applicable to tropical regions.
The model is expressed by the following equation:

\[ G(d, f, \theta, \beta) = G_{a}G_{f}G_{\theta}G_{\beta} \]  

where

\[ G_{a} = a(1 - e^{-bd}) \]
\[ a = 0.7755 A_{s} + 0.3374 f + e^{-0.164 A_{s}} \]
\[ b = 0.1584 f + e^{-0.03164 A_{s}} \]
\[ G_{f} = 1.006 e^{-0.0015f} - 0.395 e^{-0.473f} \]
\[ G_{\theta} = 0.389(f + \theta - 0.083) \]
\[ G_{\beta} = -0.000001 \beta + 0.9877 \]  

3. Data Collection

Two locations, namely IIUM Gombak and UKM Bangi are proposed to analysis site
diversity. The coordinates are 3.2528°N, 101.7372°E and 2.91972°N 101.78139°E for IIUM and
UKM respectively. The distance between IIUM and UKM is determined according to formula of
great-circle distance for two points. The great-circle distance is defined as the straight distance
between 2 points based on their coordinates. The distance is equal to 37.36 km. The rain intensity at IIUM and UKM are used for evaluation the site diversity technique. The rain rate at IIUM and UKM are measured from January 1, 2015 to December 31, 2015 concurrently using real-time rain gauges.

4. Analysis of Rain Rate Data

Out of 381 considerable raining events on both sites, only ten of these events were concurrently and they are depicted in Table 1.

<table>
<thead>
<tr>
<th>Event date</th>
<th>IIUM</th>
<th>UKM</th>
</tr>
</thead>
<tbody>
<tr>
<td>13/2/2015</td>
<td>19:28 pm until 19:57 pm</td>
<td>19:46 pm until 21:54 pm</td>
</tr>
<tr>
<td>21/3/2015</td>
<td>17:40 pm until 18:40 pm</td>
<td>17:39 pm until 17:53 pm</td>
</tr>
<tr>
<td>19/4/2015</td>
<td>18:15 pm until 19:32 pm</td>
<td>19:01 pm until 19:06 pm</td>
</tr>
<tr>
<td>1/6/2015</td>
<td>17:24 pm until 17:52 pm</td>
<td>17:43 pm until 18:38 pm</td>
</tr>
<tr>
<td>2/6/2015</td>
<td>14:04 pm until 15:09 pm</td>
<td>14:53 pm until 15:35 pm</td>
</tr>
<tr>
<td>4/8/2015</td>
<td>00:48 am until 01:28 am</td>
<td>01:12 am until 01:47 am</td>
</tr>
<tr>
<td>5/11/2015</td>
<td>14:30 pm until 15:33 pm</td>
<td>14:42 pm until 14:58 pm</td>
</tr>
<tr>
<td>13/11/2015</td>
<td>13:37 pm until 14:52 pm</td>
<td>13:40 pm until 13:57 pm</td>
</tr>
<tr>
<td>15/11/2015</td>
<td>13:11 pm until 13:18 pm</td>
<td>13:11 pm until 13:17 pm</td>
</tr>
<tr>
<td>25/11/2015</td>
<td>07:52 am until 9:11 am</td>
<td>07:45 am until 08:11 am</td>
</tr>
</tbody>
</table>

The Table 1 points out the overlapping rain events over one year and their details such as date and time of occurrence for both sides at IIUM and UKM.

Figure 2 and 3 show these simultaneous rainfall events as a function of time in both locations. Figure 3 presents the first instantaneous event dated on February 13, 2015. From this figure, it is observed that the highest value of rainfall intensity during overlapping time at IIUM is 24 mm/h which is double the observed reading at UKM (12 mm/h). This result supports the idea of site diversity mitigation technique to overcome rain attenuation.

According to Figure 3, the range of falling rain rate is from 0 mm/h to 36 mm/h at IIUM campus while it is minimum 0 mm/h to maximum 12 mm/h in the span of the whole event at UKM campus.
For all overlapping events, it can be observed that only ten concurrent events are found between IIUM and UKM out of 381 events measured in both sides. Although, the author in [21] reported that the rain cell size in tropical area is less than 15 km, but measurement shows that it reached up to 37 Km. During ten simultaneous events lowest intensity is found 6 mm/h in UKM site while 156 mm/hr is observed in IIUM site. Lowest rain intensities are found 6, 12 and 18 mm/hr during overlapping time. These rain intensities are considered as predominant impairments to weaken the satellite signal performance using site diversity between these two stations.

Period of simultaneously occurred ten rainfall events are presented in Table 2. For the one year data, concurrent time of 113 minutes is collected. Out of these overlapping time, rain intensity of 6 mm/h is occurred for a period of 85 minutes, 12 mm/hr for 26 minutes and 18 mm/h for 2 minutes are recorded. Outage probabilities of these rain intensities are calculated and presented in Table 2. Based on the value of outage probabilities, the link availability can be achieved around 99.99% by designing the link considering rain rate of 6 mm/hr at 0.01%. Preliminary results on the performance of site diversity indicate that diversity technique could be applied between two locations (IIUM and UKM campuses) to obtain the highest link availability. Separation distance which is larger than rain cell size reduces the probability of concurrent rain events at both locations, as a result, a high diversity gain as the separation distance increases.

Table 2. Duration and outage probability of simultaneously occurred rainfall

<table>
<thead>
<tr>
<th>Overlapping period</th>
<th>6 mm/h</th>
<th>12 mm/h</th>
<th>18 mm/h</th>
</tr>
</thead>
<tbody>
<tr>
<td>Figure 5.15 (8 minutes)</td>
<td>6</td>
<td>2</td>
<td>-</td>
</tr>
<tr>
<td>Figure 5.16 (14 minutes)</td>
<td>11</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>Figure 5.17 (6 minutes)</td>
<td>3</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>Figure 5.18 (10 minutes)</td>
<td>8</td>
<td>2</td>
<td>-</td>
</tr>
<tr>
<td>Figure 5.19 (17 minutes)</td>
<td>10</td>
<td>7</td>
<td>-</td>
</tr>
<tr>
<td>Figure 5.20 (10 minutes)</td>
<td>10</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Figure 5.21 (13 minutes)</td>
<td>9</td>
<td>4</td>
<td>-</td>
</tr>
<tr>
<td>Figure 5.21 (14 minutes)</td>
<td>11</td>
<td>3</td>
<td>-</td>
</tr>
<tr>
<td>Figure 5.23 (7 minutes)</td>
<td>5</td>
<td>2</td>
<td>-</td>
</tr>
<tr>
<td>Figure 5.24 (14 minutes)</td>
<td>12</td>
<td>2</td>
<td>-</td>
</tr>
<tr>
<td>Total</td>
<td>85</td>
<td>26</td>
<td>2</td>
</tr>
<tr>
<td>Probability in percentage</td>
<td>0.0162</td>
<td>0.00497</td>
<td>0.000381</td>
</tr>
</tbody>
</table>

5. Site Diversity Analysis and Discussion

The cumulative distribution of measured rain rate at IIUM and that of jointly between IIUM and UKM are analysed based on diversity concept and shown in Figure 4. Joint distribution only includes three values 6, 12 and 18 mm/h, which have probability of 0.0162%, 0.00497% and 0.000381% respectively. Rain rate distribution measured at IIUM and that measured jointly at IIUM and UKM are converted to rain attenuation distribution using proposed model [22] as shown in Figure 5. This figure depicts comparison between rain attenuation at IIUM and diversity between IIUM and UKM.
In order to analyse site diversity gain model, MEASAT3 (geostationary at 91.5°E) is assumed as reference satellite and Kulliyyah of Engineering, International Islamic University Malaysia (3.2528°N, 101.7372°E) is assumed as reference base station and Faculty of Engineering, UKM (2.91972°N 101.78139°E) as diversity station. Table 3 shows the technical parameters of the system.

Table 3. Technical parameters of the outdoor system.

<table>
<thead>
<tr>
<th>Ground Station Location</th>
<th>3.2528°N, 101.7372°E</th>
</tr>
</thead>
<tbody>
<tr>
<td>Satellite Position</td>
<td>91.5° E</td>
</tr>
<tr>
<td>Azimuth Angle</td>
<td>253°</td>
</tr>
<tr>
<td>Elevation Angle</td>
<td>77.4°</td>
</tr>
<tr>
<td>Polarization</td>
<td>Vertical</td>
</tr>
<tr>
<td>Frequency</td>
<td>12 GHz</td>
</tr>
</tbody>
</table>
Diversity gain are calculated based on Hodge (2), ITU-R (4), Panagopoulos (6) and Semire (10) prediction models using parameters given in Table 3 and those measured from Figure 4 and 5 and presented in Figure 6 and Figure 7 for baseline angles of 90° and 0° respectively. The result indicates that the measured site diversity gain is very close to that predicted by ITU-R and Hodge model for baseline angle of 90° with 37.36 km separation and MEASAT3 as reference satellite. Predictions by Semire underestimates the measurement 8 dB and 6 dB at single site fade of 32 dB and 22 dB respectively; while Panagopoulos underestimates 5 dB and 3 dB for single site fade of 32 and 22 dB respectively. However, all models underestimate the measurement for baseline angle of 0°.

Figure 6. Comparison of site diversity gain prediction models with measured site diversity gain for base line orientation of 90 degree in Kuala Lumpur, Malaysia.

Figure 7. Comparison of site diversity gain prediction models with measured site diversity gain for base line orientation of 0 degree in Kuala Lumpur, Malaysia.

4. Conclusion
Site diversity technique is analyzed based on 1-minute rain rate measurements in two locations separated by 37.36 Km in Malaysia for one year period. From analysis, it is found that 10 raining events occurred concurrently in both sites out of 381 measured events in a year. By analyzing all overlapping raining events, joint probability distribution was calculated and found three values of 6, 12 and 18 mm/h, are 0.0162%, 0.00497% and 0.000381% respectively. In order to investigate diversity gain, measured rain rate distribution is converted to rain attenuation distribution using proposed model and compare with those predicted by ITU-R, Hodge, Panagopoulos and Semire prediction models. The result indicates that the measured site diversity gain is very close to that predicted by ITU-R and Hodge model for baseline angle of 90 with 37.36 km separation and MEASAT3 as reference satellite. Predictions by Semire...
agopoulos underestimates 5 dB and 3 dB for single site fade of 32 and 22 dB respectively; while Panagopoulos underestimates 5 dB and 3 dB for single site fade of 32 and 22 dB respectively. However, all models underestimate the measurement for baseline angle of 0°. These findings will be very useful for Earth-to-satellite link designers to improve reliability by applying site diversity as a rain fade mitigation technique at any frequency.

References


