

Voltage Profile Enhancement and Reduction of Real Power Loss by Hybrid Biogeography Based Artificial Bee Colony algorithm

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Abstract

This paper presents Hybrid Biogeography algorithm for solving the multi-objective reactive power dispatch problem in a power system. Real Power Loss minimization and maximization of voltage stability margin are taken as the objectives. Artificial bee colony optimization (ABC) is quick and forceful algorithm for global optimization. Biogeography-Based Optimization (BBO) is a new-fangled biogeography inspired algorithm. It mainly utilizes the biogeography-based relocation operator to share the information among solutions. In this work, a hybrid algorithm with BBO and ABC is projected, and named as HBBABC (Hybrid Biogeography based Artificial Bee Colony Optimization), for the universal numerical optimization problem. HBBABC merge the searching behavior of ABC with that of BBO. Both the algorithms have different solution probing tendency like ABC have good exploration probing tendency while BBO have good exploitation probing tendency. HBBABC used to solve the reactive power dispatch problem and the proposed technique has been tested in standard IEEE30 bus test system.

Keywords: Modal analysis, optimal reactive power, Transmission loss, Artificial Bee Colony Algorithm, Hybrid Biogeography

1. Introduction

Optimal reactive power dispatch problem is one of the hard optimization problems in power system. The problem that has to be solved in a reactive power optimization is to decide on the required reactive generation at various locations so as to optimize the objective function. Here the reactive power dispatch problem engages about best utilization of the existing generator bus voltage magnitudes, transformer tap setting and the output of reactive power sources so as to minimize the real power loss and to augment the voltage stability of the system. Various mathematical techniques have been implemented to solve this optimal reactive power dispatch problem. These include the gradient method [1-2], Newton method [3] and linear programming [4-7]. The gradient and Newton methods experience from the intricacy in handling inequality constraints. Recently global Optimization techniques such as genetic algorithms have been proposed to solve the reactive power flow problem [8, 9]. Hybridization of algorithm means to merge the capabilities of different algorithm in a single algorithm. Hybridization is done to triumph over the drawback in the existing algorithms and to obtain superior solutions. Evolutionary Algorithms (EAs) are much admired for the hybridization due to their dissimilar capabilities in handling different types of problems. Continuous research is going on to find new optimization techniques which are able to handling variety of problems with high effectiveness, efficiency and flexibility and thus there are many such optimization algorithms like GA, SA, DE, PSO, ACO, SFLA, ABC, BBO etc. Hybridization is one of the admired methods to augment the effectiveness, efficiency and flexibility of the algorithm to create better solution and convergence rates and minimizing computational times. Many such amalgam algorithms are available in the literature and continuous efforts are sustained to develop new hybrid algorithms. ABC (artificial bee colony) [15]-[18] is a straightforward and commanding population-based algorithm for finding the global optimum solutions. ABC separate the population in two key parts viz. employed bees and onlooker bees. Employed bees begin explore with precise rules and onlooker bees go behind the employed bees in analogous to the fitness of employed bees and it also revise the solution as employed bees. If there is no change in the fitness of employed bees for some number of generations then that bee is transformed in scout bee which starts for a

new-fangled search and acts as an employed bee from then. Algorithm prolong for predefined number of generations or until the best solution is found. So ABC finds the universal solution by exploring the search space with specific rules followed by employed bees, onlooker bees and scout bees. Biogeography-Based Optimization (BBO), proposed by Simon [27], a novel global optimization algorithm based on the biogeography theory, and it is the study about the distribution of species. BBO [28]-[30] is also population-based optimization system. In the original BBO algorithm, every solution of the population is a vector of integers. BBO updates the solution subsequent to immigration and emigration phenomenon of the species from one place to the other which is referred as islands by Simon. BBO has high-quality exploitation ability as solution and is updated by exchanging the existing design variables among the solution. In order to merge the searching capabilities of ABC and BBO, in this paper, we plan a hybrid ABC with BBO, referred to as HBBABC, for solving the optimal reactive power dispatch problem. In HBBABC, algorithm begins by updating the solutions utilizing the immigration and emigration rates. Solution is further customized by using the exploration propensity of ABC using employed, onlooker and scout bees.

2. Voltage Stability Evaluation

Modal analysis for voltage stability evaluation

The linearized steady state system power flow equations are given by,

$$\begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix} = \begin{bmatrix} J_{p\theta} J_{pv} \\ J_{q\theta} J_{qv} \end{bmatrix} \quad (1)$$

Where

ΔP = Incremental change in bus real power.

ΔQ = Incremental change in bus reactive

Power injection

$\Delta \theta$ = incremental change in bus voltage angle.

ΔV = Incremental change in bus voltage Magnitude

$J_{p\theta}$, J_{pv} , $J_{q\theta}$, J_{qv} jacobian matrix are the sub-matrixes of the System voltage stability is affected by both P and Q. On the other hand at each operational point we keep P constant and evaluate voltage stability by taking into account of incremental relationship between Q and V.

To reduce (1), let $\Delta P = 0$, then.

$$\Delta Q = [J_{qv} - J_{q\theta} J_{p\theta}^{-1} J_{pv}] \Delta V = J_R \Delta V \quad (2)$$

$$\Delta V = J^{-1} - \Delta Q \quad (3)$$

Where

$$J_R = (J_{qv} - J_{q\theta} J_{p\theta}^{-1} J_{pv}) \quad (4)$$

J_R is called the reduced Jacobian matrix of the system.

Modes of Voltage instability:

Voltage Stability characteristics are computed by the Eigen values and Eigen vectors.

Let

$$J_R = \xi \Lambda \eta \quad (5)$$

Where,

ξ = right eigenvector matrix of J_R

η = left eigenvector matrix of J_R

Λ = diagonal Eigen value matrix of J_R and

$$J_{R^{-1}} = \xi \Lambda^{-1} \eta \quad (6)$$

From (3) and (6), we have

$$\Delta V = \xi \Lambda^{-1} \eta \Delta Q \quad (7)$$

or

$$\Delta V = \sum_i \frac{\xi_i \eta_i}{\lambda_i} \Delta Q \quad (8)$$

Where ξ_i is the i th column right Eigen vector and η the i th row left eigenvector of J_R .

λ_i is the i th eigen value of J_R .

The i th modal reactive power variation is,

$$\Delta Q_{mi} = K_i \xi_i \quad (9)$$

where,

$$K_i = \sum_j \xi_{ij}^2 - 1 \quad (10)$$

Where

ξ_{ji} is the j th element of ξ_i

The corresponding i th modal voltage variation is

$$\Delta V_{mi} = [1/\lambda_i] \Delta Q_{mi} \quad (11)$$

In (8), let $\Delta Q = e_k$ where e_k has all its elements zero except the k th one being 1. Then,

$$\Delta V = \sum_i \frac{\eta_{1k} \xi_i}{\lambda_i} \quad (12)$$

η_{1k} k th element of η_1

V-Q sensitivity at bus k

$$\frac{\partial V_k}{\partial Q_k} = \sum_i \frac{\eta_{1k} \xi_i}{\lambda_i} = \sum_i \frac{P_{ki}}{\lambda_i} \quad (13)$$

3. Problem Formulation

The objective of the reactive power dispatch problem considered here is to reduce the real power loss and to enhance the static voltage stability margins (SVSM).

Minimization of Real Power Loss

Minimization of the real power loss (Ploss) in transmission lines of a power system is mathematically stated as follows.

$$P_{loss} = \sum_{k=1}^n g_k (V_i^2 + V_j^2 - 2V_i V_j \cos \theta_{ij}) \quad (14)$$

Where n is the number of transmission lines, g_k is the conductance of branch k , V_i and V_j are voltage magnitude at bus i and bus j , and θ_{ij} is the voltage angle difference between bus i and bus j .

Minimization of Voltage Deviation

Minimization of the Deviations in voltage magnitudes (VD) at load buses is mathematically stated as follows.

$$\text{Minimize } VD = \sum_{k=1}^{nl} |V_k - 1.0| \quad (15)$$

Where nl is the number of load busses and V_k is the voltage magnitude at bus k .

System Constraints

Objective functions are subjected to these constraints shown below.

Load flow equality constraints:

$$P_{Gi} - P_{Di} - V_i \sum_{j=1}^{nb} V_j \begin{bmatrix} G_{ij} & \cos \theta_{ij} \\ +B_{ij} & \sin \theta_{ij} \end{bmatrix} = 0, i = 1, 2, \dots, nb \quad (16)$$

$$Q_{Gi} - Q_{Di} V_i \sum_{j=1}^{nb} V_j \begin{bmatrix} G_{ij} & \cos \theta_{ij} \\ +B_{ij} & \sin \theta_{ij} \end{bmatrix} = 0, i = 1, 2, \dots, nb \quad (17)$$

where, nb is the number of buses, PG and QG are the real and reactive power of the generator, PD and QD are the real and reactive load of the generator, and G_{ij} and B_{ij} are the mutual conductance and susceptance between bus i and bus j .

Generator bus voltage (V_{Gi}) inequality constraint:

$$V_{Gi}^{\min} \leq V_{Gi} \leq V_{Gi}^{\max}, i \in ng \quad (18)$$

Load bus voltage (V_{Li}) inequality constraint:

$$V_{Li}^{\min} \leq V_{Li} \leq V_{Li}^{\max}, i \in nl \quad (19)$$

Switchable reactive power compensations (Q_{Ci}) inequality constraint:

$$Q_{Ci}^{\min} \leq Q_{Ci} \leq Q_{Ci}^{\max}, i \in nc \quad (20)$$

Reactive power generation (Q_{Gi}) inequality constraint:

$$Q_{Gi}^{\min} \leq Q_{Gi} \leq Q_{Gi}^{\max}, i \in ng \quad (21)$$

Transformers tap setting (T_i) inequality constraint:

$$T_i^{\min} \leq T_i \leq T_i^{\max}, i \in nt \quad (22)$$

Transmission line flow (S_{Li}) inequality constraint:

$$S_{Li}^{\min} \leq S_{Li} \leq S_{Li}^{\max}, i \in nl \quad (23)$$

Where, nc , ng and nt are numbers of the switchable reactive power sources, generators and transformers.

4. Biogeography-Based Optimization (BBO)

BBO is a new population-based optimization algorithm stimulated by the natural biogeography distribution of dissimilar species. In BBO, every entity is considered as a "habitat" with a habitat suitability index (HSI). A high-quality solution is analogous to an island with a high HSI, and a poor solution indicates an island with a low HSI. High HSI solutions are inclined to share their features with low HSI solutions. Low HSI solutions admit lot of novel features from high HSI solutions. In BBO, each individual has its own immigration rate λ and emigration rate μ . A high-quality solution has higher μ and lower λ and vice versa. The immigrant ion rate and the emigration rate are functions of the amount of species in the habitat. They can be calculated as follows,

$$\lambda_k = I \left(1 - \frac{k}{n}\right) \quad (24)$$

$$\mu_k = E \left(\frac{k}{n}\right) \quad (25)$$

Where I is the maximum possible immigration rate; E is the maximum possible emigration rate; k is the number of species of the k -th individual; and n is the maximum number of species. In BBO, there are two key operators, the migration and the mutation.

Migration

Consider a population of contestant which is represented by a design variable. Every design variable for particular population member is measured as SIV for that population member. Every population member is considered as individual habitat or Island. The objective function value point out the HSI for the particular population member. The emigration and immigration rates of every solution are used to probabilistically distribute information between habitats. If a given solution is chosen for modification, then its immigration rate λ is used to probabilistically alter each suitability index variable (SIV) in that solution. If a given SIV in a given solution S_i is selected for the modification, then its emigration rates μ of the other solutions is used to probabilistically decide which of the solutions should migrate. And it is randomly selected SIV to solution S_i . The above occurrence is known as migration in BBO.

Mutation

In nature a habitat's HSI can vary abruptly due to arbitrary events. This phenomenon is termed as SIV mutation, and probabilities of species count are used to decide mutation rates. This possibility mutates low HSI as well as high HSI solutions. Mutation of high HSI solutions gives them the possibility to further improvement. Mutation rate is obtained using following equation.

$$M(s) = m_{\max} \left(1 - \frac{P_s}{P_{\max}}\right) \quad (26)$$

Where, m_{\max} is a user-defined parameter called mutation coefficient.

5. Artificial Bee Colony (ABC) technique

Artificial Bee Colony (ABC) Algorithm is an optimization algorithm based on the intellectual foraging behavior of honey bee swarm. The colony of artificial bees consists of three groups of bees: employed bees, onlookers and scouts. An employed bee searches the target where the food is available. They accumulate the food and returns back to its source where they carry out waggle dance depending on the amount of food available at the target. The onlooker bee observe the dance and follows employed bee depends on the probability of the available food means more onlooker bee will follow the employed bee associated with the target having more amount of food. The employed bee whose food source becomes abandoned then it changes into a scout bee and it will search for the new food source. For solving optimization problems the population is alienated into two parts consisting of employed bees and onlooker bees. An employed bee searches the solution in the explore space and the value of objective function associated with the solution is the amount of food linked with that solution. Employed bee updates its position using Equation (27) and it updates new position if it is better than the preceding position.

$$v_{ij} = x_{ij} + R_{ij}(x_{ij} - x_{kj}) \quad (27)$$

Where v_{ij} is the new position of employee bee, x_{ij} is the current position of employed bee, k is a random number between $(1, N \text{ (population size)}/2) \neq i$ and $j = 1, 2, \dots$, Number of design variables. R_{ij} is a random number between $(-1, 1)$.

An onlooker bees prefer a food source depending on the probability value related with that food source, p_i , calculated using Equation (28).

$$P_i = \frac{F_i}{\sum_{n=1}^{N/2} F_n} \quad (28)$$

Where F_i is the fitness value of the solution i and $N/2$ is the number of food sources which is equal to the number of employed bees.

The Employed bee whose location of the food source cannot be enhanced for some predetermined number of cycles than that food source is called abandoned food source. That employed bee becomes scout and searches for the new solution randomly using Equation (29).

$$x_i^j = x_{\min}^j + \text{rand}(0,1)(x_{\max}^j - x_{\min}^j) \quad (29)$$

6. HBBABC: Hybrid Biogeography Based Artificial Bee Colony Optimization

ABC is superior at exploring the search space and locating the region of global minimum. On the other hand, BBO has a high-quality exploitation searching tendency for global optimization. Based on these considerations, in order to capitalize on the exploration and the exploitation HBBABC approach is projected. Step by step methodology for the implementation of HBBABC for solving optimal reactive power dispatch problem is given as follows.

Step 1: Initialize BBO and ABC parameters which are essential for the algorithm to progress. These parameters include population size, number of generations essential for the termination criteria, Maximum immigration and emigration rates, number of design variables and relevant range for the design variables.

Step 2: produce arbitrary population equal to the population size. Each population member has the value of all the design variables. This value of design variable is arbitrarily generated in between the design variable range specified. Each design variable in the population indicates SIVs for that particular population member (Habitat).

Step 3: acquire the value of objective function for all population members. The value of objective function so obtained designates the HSI for that Habitat (population member).

Step 4: plot the value of HSI to obtain the species count. For reactive power dispatch optimization problem is of minimization type than low HSI member is given high species count.

Step 5: alter population by using the migration operator considering its immigration and emigration rates. If a given solution is selected to be customized, then its immigration rate λ is used to probabilistically modify each suitability index variable (SIV) in that solution. If a given SIV in a given solution S_i is selected to be modified, then its emigration rates μ of the other solutions is used to probabilistically decide which of the solutions should migrate its randomly selected SIV to solution S_i . Code for migration is given in figure 1.

```

For  $i = 1$  to  $NP$  Choose  $X_i$  with probability relative to  $\lambda_i$ 
If  $\text{rand}(0, 1) < \lambda_i$ 
For  $j = 1$  to  $NP$ 
Choose  $X_j$  with probability relative to  $\mu_j$ 
If  $\text{rand}(0, 1) < \mu_j$ 
Arbitrarily select a variable  $\sigma$  from  $X_j$ 
Reinstate the corresponding variable in  $X_i$  with  $\sigma$ 
End if
End

```

Figure 1. Code for migration

Step 6: separate the population into two equal parts to act as employed bees and onlooker bees. Attain the value of objective function for employed bees. The value of objective function so obtained indicates the amount of nectar (food) associated with that target (food source).

Step 7: renew the location of employed bees using Equation (27). If the value of objective function of the new solution is superior to the existing solution, reinstate the existing solution with the new one.

Step 8: compute probability related with the different solutions using Equation (28). Onlooker bee goes behind a solution depending on the probability of that solution. So more the probability of the solution more will be the onlooker bee following that solution.

Step 9: renew the position of onlooker bees using Equation (27). If the rate of objective function of the new solution is better than the existing solution, reinstate the existing solution with the new one.

Step 10: discover abandon solution and reinstate it with the newly generated solution using Equation (29).

Step 11: carry on all the steps from step 3 until the specified number of generations are reached.

Detailed HBBABC code applied to optimal reactive power dispatch problem is given in figure 2

```

START
Initialize essential parameters necessary for the algorithm .create
the initial population N, calculate the fitness for each individual
in N.
For i=1 to number of generations
BBO loop
For every individual, plot the fitness to the number of species
Compute the immigration rate  $\lambda_i$  and the emigration rate  $\mu_i$  for
every individual  $X_i$ 
For i= 1 to N
Choose  $X_i$  with probability proportional to  $\lambda_i$ 
If rand (0, 1) <  $\lambda_i$ 
For j= 1 to N
Choose  $X_j$  with probability proportional to  $\mu_j$ 
If rand (0, 1) <  $\mu_j$ 
Arbitrarily select a variable  $\sigma$  from  $X_j$ 
Reinstate the corresponding variable in  $X_i$  with  $\sigma$ 
End if
End
ABC loop
For i= 1 to N/2
Create new-fangled solutions  $v_{ij}$  for the employed bees and
appraise them
Reinstate new-fangled solution if it is better than the preceding
one
End
Compute the probability values  $p_{ij}$  for the solutions and
recognize onlooker bees depending on the probability  $p_{ij}$ 
For i= 1 to N/2
Create the new-fangled solutions  $v_{ij}$  for the onlookers and
reinstate new solution if it is better than the preceding one
End
Find out the abandoned solution for the scout, if exists, and
reinstate it with a new randomly produced solution  $x_{ij}$ 
End
STOP

```

Figure 2. HBBABC code for solving optimal reactive power dispatch problem

7. Simulation Results

The performance of the proposed HBBABC method is demonstrated by testing it on standard IEEE-30 bus system. The IEEE-30 bus system has 6 generator buses, 24 load buses and 41 transmission lines of which four branches are (6-9), (6-10), (4-12) and (28-27) - are with the tap setting transformers. The lower voltage magnitude limits at all buses are 0.95 p.u. and the upper limits are 1.1 for all the PV buses and 1.05 p.u. for all the PQ buses and the reference bus. The simulation results have been presented in Tables 1, 2, 3 & 4. And in the Table 5 shows the proposed algorithm powerfully reduces the real power losses when compared to other given algorithms. The optimal values of the control variables along with the minimum loss obtained

are given in Table 1. Corresponding to this control variable setting, it was found that there are no limit violations in any of the state variables.

Table 1. Results of HBBABC – ORPD optimal control variables

Control variables	Variable setting
V1	1.043
V2	1.041
V5	1.040
V8	1.033
V11	1.004
V13	1.041
T11	1.04
T12	1.02
T15	1.0
T36	1.0
Qc10	3
Qc12	4
Qc15	4
Qc17	0
Qc20	3
Qc23	3
Qc24	2
Qc29	3
Real power loss	4.3258
SVSM	0.2471

ORPD together with voltage stability constraint problem was handled in this case as a multi-objective optimization problem where both power loss and maximum voltage stability margin of the system were optimized simultaneously. Table 2 indicates the optimal values of these control variables. Also it is found that there are no limit violations of the state variables. It indicates the voltage stability index has increased from 0.2471 to 0.2483, an advance in the system voltage stability. To determine the voltage security of the system, contingency analysis was conducted using the control variable setting obtained in case 1 and case 2. The Eigen values equivalents to the four critical contingencies are given in Table 3. From this result it is observed that the Eigen value has been improved considerably for all contingencies in the second case.

Table 2. Results of HBBABC-Voltage Stability Control Reactive Power Dispatch Optimal Control Variables

Control Variables	Variable Setting
V1	1.045
V2	1.044
V5	1.03
V8	1.034
V11	1.006
V13	1.036
T11	0.090
T12	0.090
T15	0.090
T36	0.090
Qc10	4
Qc12	3
Qc15	4
Qc17	4
Qc20	0
Qc23	3
Qc24	3
Qc29	4
Real power loss	4.9789
SVSM	0.2483

Table 3. Voltage Stability under Contingency State

Sl.No	Contingency	ORPD Setting	VSCRPD Setting
1	28-27	0.1410	0.1422
2	4-12	0.1658	0.1668
3	1-3	0.1774	0.1782
4	2-4	0.2032	0.2053

Table 4. Limit Violation Checking Of State Variables

State variables	limits		ORPD	VSCRPD
	Lower	upper		
Q1	-20	152	1.3422	-1.3269
Q2	-20	61	8.9900	9.8232
Q5	-15	49.92	25.920	26.001
Q8	-10	63.52	38.8200	40.802
Q11	-15	42	2.9300	5.002
Q13	-15	48	8.1025	6.033
V3	0.95	1.05	1.0372	1.0392
V4	0.95	1.05	1.0307	1.0328
V6	0.95	1.05	1.0282	1.0298
V7	0.95	1.05	1.0101	1.0152
V9	0.95	1.05	1.0462	1.0412
V10	0.95	1.05	1.0482	1.0498
V12	0.95	1.05	1.0400	1.0466
V14	0.95	1.05	1.0474	1.0443
V15	0.95	1.05	1.0457	1.0413
V16	0.95	1.05	1.0426	1.0405
V17	0.95	1.05	1.0382	1.0396
V18	0.95	1.05	1.0392	1.0400
V19	0.95	1.05	1.0381	1.0394
V20	0.95	1.05	1.0112	1.0194
V21	0.95	1.05	1.0435	1.0243
V22	0.95	1.05	1.0448	1.0396
V23	0.95	1.05	1.0472	1.0372
V24	0.95	1.05	1.0484	1.0372
V25	0.95	1.05	1.0142	1.0192
V26	0.95	1.05	1.0494	1.0422
V27	0.95	1.05	1.0472	1.0452
V28	0.95	1.05	1.0243	1.0283
V29	0.95	1.05	1.0439	1.0419
V30	0.95	1.05	1.0418	1.0397

Table 5. Comparison of Real Power Loss

Method	Minimum loss
Evolutionary programming[10]	5.0159
Genetic algorithm[11]	4.665
Real coded GA with Lindex as SVSM[12]	4.568
Real coded genetic algorithm[13]	4.5015
Proposed HBBABC method	4.3258

8. Conclusion

In this paper a novel approach HBBABC algorithm used to solve optimal reactive power dispatch problem. The performance of the proposed algorithm demonstrated through its voltage stability assessment by modal analysis is effective at various instants following system contingencies. Real power loss has been reduced considerably and voltage profiles has been enhanced.

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